

MTH 150 Chapter 4

Alejandro Franco

October 29, 2021

1 Reflection

When it came to this chapter i had to refresh my memory on logarithm functions and properties for this section i relied heavy on my graphing calculator for help.

I had a little bit of trouble in section 4.1 and 4.2 at first because i had forgotten most rules for logs. Once i looked back at the expressions i was able to complete this section quite easily

I found section 4.3 really easy as all i had to do was use the expression $b^a = c$ rewrite all the logarithm equations

As for section 4.4 i found it o be most difficult as knowing the differences in the logs was a bit complicated for me. I had to refer back to the answer solution to double check my work.Im still a bit unsure of how the use the expressions

In section 4.5 i found it to be pretty easy since i used my calculator to graph the log functions to figure out its domain and vertical asymptote

2 Section 4.1 Exponential Functions

2.1 7,13,23

1. A population numbers 11,000 organisms initially and grows by 8.5 percent each year. Write an exponential model for the population.

$$F(x) = ab^x$$

$$b = (1 + r)$$

$$b = 1.085$$

$$f(x) = 11,000(1.085)^x$$

- .Find a formula for an exponential function passing through the two points. (0,6), (3,750)

$$(0, 6), (3, 750)$$

$$f(x) = ab^x$$

$$f(0) = ab^0$$

$$f(0) = 6$$

$$a = 6$$

$$f(x) = 6b^x$$

$$\text{plugin750}$$

$$750 = 6(b)^3 = b = 5$$

$$f(x) = 6(5)^x$$

- 23** Describe the long run behavior, as $x \rightarrow$ and $x \rightarrow$ of each function

$$f(x) = -5(4^x) - 1$$

As x approaches ∞ $f(x)$ approaches $-\infty$

As x approaches ∞ $f(x)$ approaches $-\infty$

4^x is multiplied by a negative

Comments

This was pretty simple, after having a refresher on the subject this section i found to be very easy.

3 Section 4.2 Graphs of Exponential Functions

3.1 11,23

11 Sketch a graph of each of the following transformations of $f(x) = 2^x$ $f(x) = 2^x$

23 A radioactive substance decays exponentially. A scientist begins with 100 milligrams of a radioactive substance. After 35 hours, 50 mg of the substance remains. How many milligrams will remain after 54 hours?

$$f(x) = a(b)^x$$

$$a = 100$$

$$100(50)^x$$

$$f(x) = 100(0.98031)^x$$

$$f(x) = 100(0.98031)^{54}$$

$$f(x) = 33.58 \text{ milligrams}$$

Comments

This was pretty simple, i had trouble though figuring out the word problems as figuring out the inputs were difficult to find.

4 Section 4.3 Logarithmic Functions

4.1 1, 9, 17, 41, 65

1 *Rewrite each equation in exponential form*

$$\log_4(q) = m$$

$$\log_b(C) = a$$

$$b^a = c$$

$$4^m = q$$

9 *Rewrite each equation in logarithmic form.*

$$4^x = y$$

$$b^a = c$$

$$\log_b C = q$$

$$\log_4 7 = x$$

17 *Solve for x.*

$$\log_3(x = 2)$$

$$b^a = c$$

$$3^2 = x$$

$$x = 9$$

41

$$b^a = C$$

$$5^x = 14$$

$$\log_5 14 = x$$

$$x = 1.639$$

65 *The population of Kenya was 39.8 million in 2009 and has been growing by about 2.6 percent each year. If this trend continues, when will the population exceed 45 million?*

$$y = ab^t$$

$$b = (1 + r)$$

$$2.6 = 1.026b$$

$$f(t) = 4.5\text{million}$$

$$45 = (39.8)(1.026)^t$$

$$\frac{45}{39.8}$$

$$4.78\text{years}$$

Comments

This was pretty simple, had to be careful when i inputting the right variables

5 Section 4.5 Graphs of Logarithmic Functions

5.1 1,2,3,4

1

$$f(x) = \log(x - 5)$$

*Domain = $x > 5$
(VA) = $x=5$*

2

$$\ln(3 - x)$$

*Domain = $x < 3$
(VA) = $x=3$*

3

$$\log(3x + 1)$$

Domain $x > -\frac{1}{3}$

$$\frac{1}{3}$$

(VA) $x = -\frac{1}{3}$

4

$$3\log(-x) + 2$$

*Domain = $x < 0$
(VA) = $x = 0$*

This was fairly simple, got a little lost when trying to find the asymptote points as it's been a while but the work was easy